

ME 297

L6 Line of sight RSS combination

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Ref. Dr. Jim Burge's Notes

LOS optical systems

- **Combining multiple contributions to system LOS**
 - Independent sources
 - Coupled sources
- **Example problems**
- **General relationship between element motion and system LOS**

Combining multiple independent sources of error

- **Many things that can go wrong that will affect system performance. To calculate the combined effect if:**
 - **Roots of cause independent combine the effects as a Root Sum Square (RSS). Good to know**
 - The answer is dominated by the biggest contributors
 - The smallest contributors are negligible
 - *For N equal contributions, the RSS is equal to square root of N times an individual contribution.*

RSS example

10 μ rad pointing from element 1

15 μ rad pointing from element 2

5 μ rad pointing from element 3

Combined effect:

$$\begin{aligned} & \sqrt{10^2 + 15^2 + 5^2} \\ &= \sqrt{100 + 225 + 25} \\ &= \sqrt{350} \\ &= 18.7 \end{aligned}$$

RSS is dominated by the largest contributors

Example:

Compute RSS of 10, 1, 2, 1, 1

$$= \text{sqrt}(100+1+4+1+1)$$

$$= 10.3 \quad (\text{not much different from } 10)$$

Small contributors do not affect RSS

Compute RSS of 10, 11, 10

$$= \text{sqrt}(100+121+100)$$

$$= 17.9$$

Now add another term of 2

$$\text{rss} = \text{sqrt}(100+121+100 + 4)$$

$$= 18.0$$

Not much different from 17.9

For terms with equal contribution

Compute RSS for N equal contributions of x :

$$\begin{aligned}RSS &= \sqrt{x^2 + x^2 + x^2 + x^2 + \dots (N \text{ times})} \\ &= \sqrt{N(x^2)} \\ &= \sqrt{N} \cdot x\end{aligned}$$

Few rules for compound systems

- With many independent degrees of freedom the optimal distribution of error may be equal contributions from each DOF.
- System performance can be improved by reducing just the dominant sources of error
- Small contributors can be relaxed to reduce the cost without changing the performance.
- When the performance is good enough, cost of improving is not justified so relax.
- Maximize use of COTS (commercial off the shelf) parts for cost reduction.

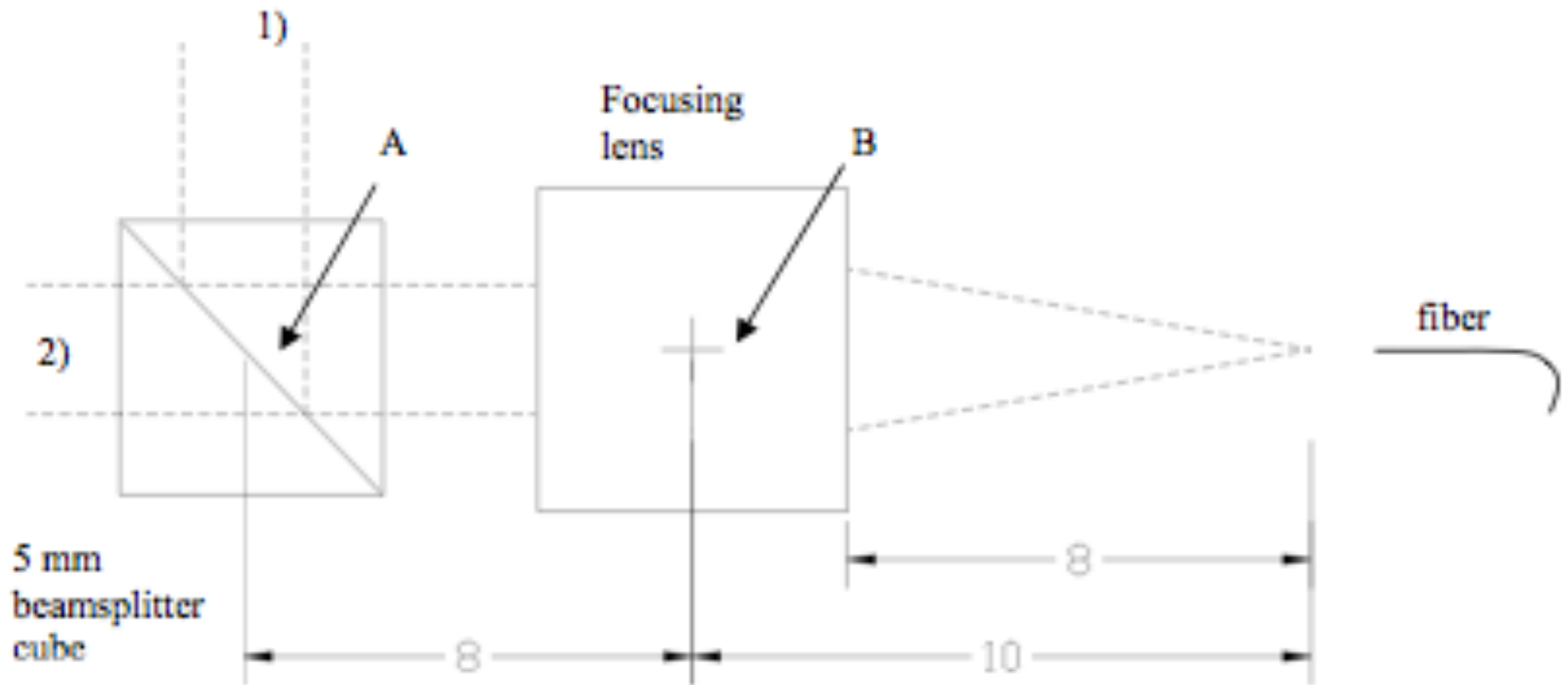
Combining errors when the effects are coupled

- If one root cause results in many changes in the system, then the errors are coupled. For example temperature change causes all the parts expand or contract.
- In these cases the root cause is treated as a degree of freedom (DOF)
- The combined effect for the whole system when the DOF changes is calculated.
- this is done by calculating each contribution and summing them up ***keeping the sign.***

Example Problem : Image stability

- Consider a simple two-channel fiber coupler shown on next page. The incident beams are 3 mm in diameter, and come to focus on the end of the fiber with 0.1 NA. The back focal distance, as shown from the focusing lens (which is a multi-element lens) to the fiber is 8 mm. Coupling efficiency requires the position and rotation of the optics to be maintained so that both focused spots (one from beam 1 and the other from beam 2) are maintained on the fiber to $\pm 0.3 \mu\text{m}$

Example Problem : Image stability



Example Problem : Image stability

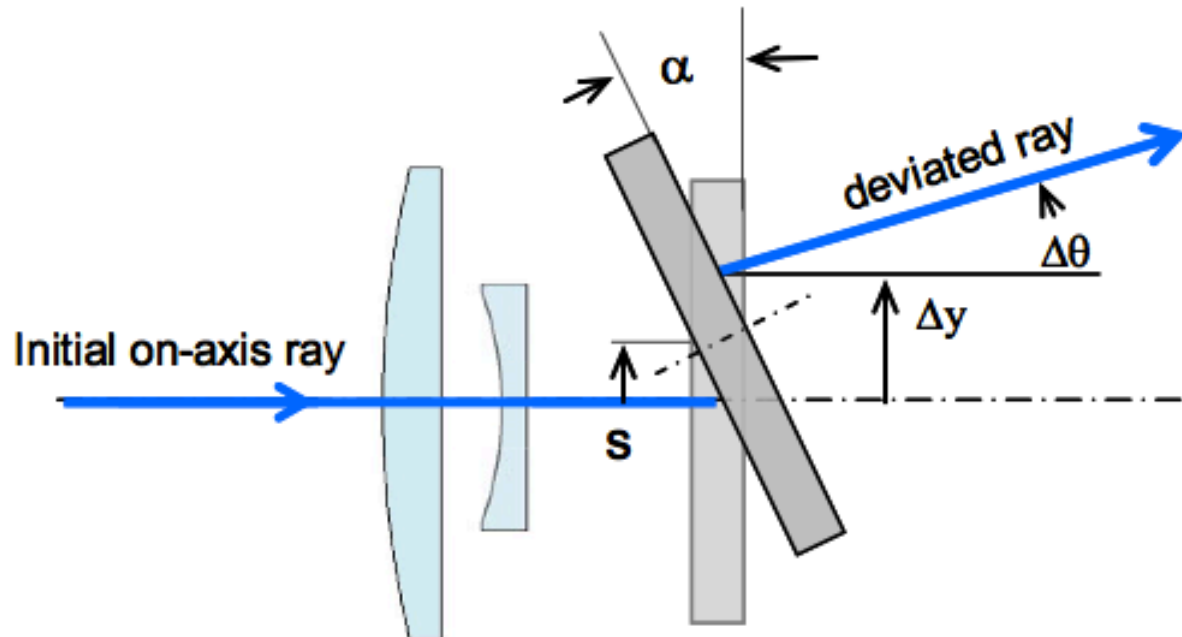
- a) Determine the focal length of the lens and find its nodal point.
Calculate the following sources of error, consider the effects for both inputs 1 and 2
- b) Lateral translation of beam splitter cube $20\ \mu\text{m}$
- c) Rotation of the beam splitter cube about point A of $3\ \mu\text{rad}$
- d) Lateral translation of the focusing lens of $0.1\ \mu\text{m}$
- e) Rotation of focusing lens about point B of $20\ \mu\text{rad}$ (decompose motion into rotation about nodal point + translation of nodal point.)
- f) Lateral translation of the fiber of $0.1\ \mu\text{m}$
- g) Calculate the combined effect of all of the above and summarize in a table like the one shown
- h) How does this compare to the requirement?

Motion	Beam 1	Beam 2	Combined for 2 beams
b)			
c)			
...			
Combined effect			

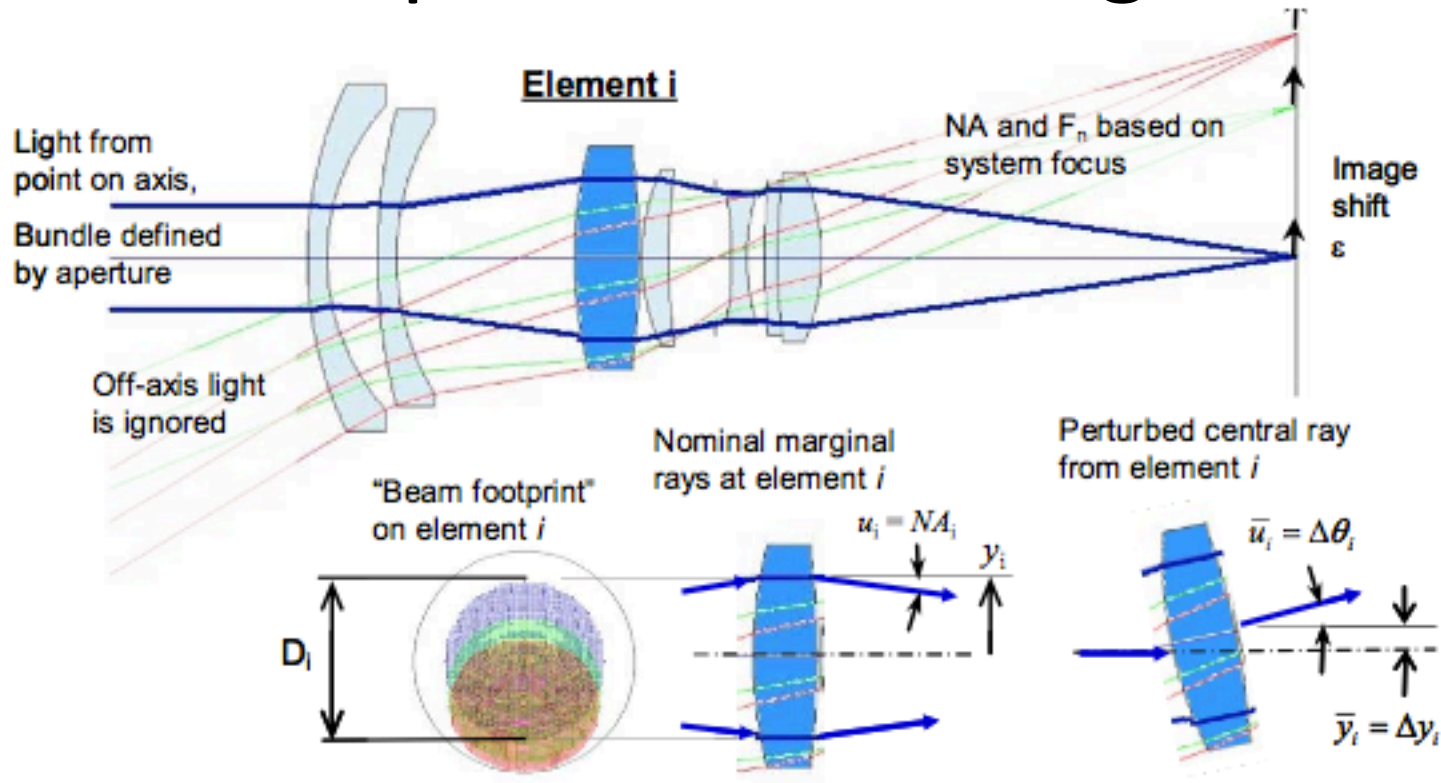
What happens when an optical element moves

To see image motion,
follow the central ray
Generally, it changes in position and angle

Element motion
 s : decenter
 α : tilt
Central ray deviation
 Δy : lateral shift
 $\Delta\theta$: change in angle



General expression for image motion



$$\epsilon = F_n D_i \Delta\theta_i - \frac{NA_i}{NA} \Delta y_i$$

F_n final working f-number = $\frac{1}{2NA}$

D_i beam footprint for on-axis bundle

$\Delta\theta_i$ = change in central ray angle due to motion of element *i*

General relationship for tilt due to element motion and image shift

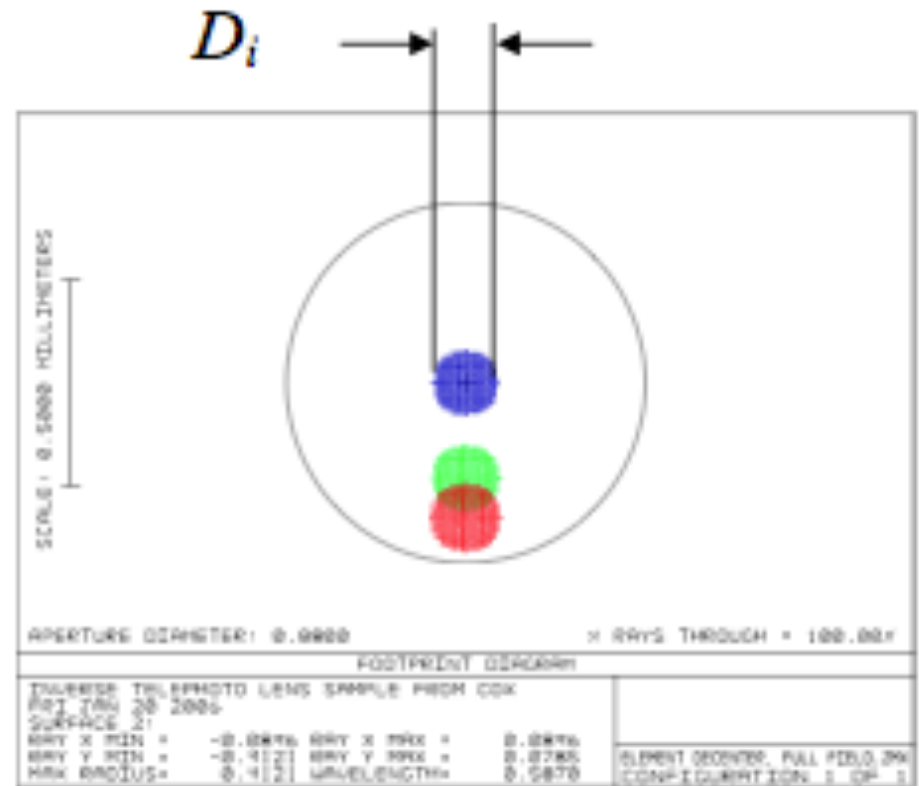
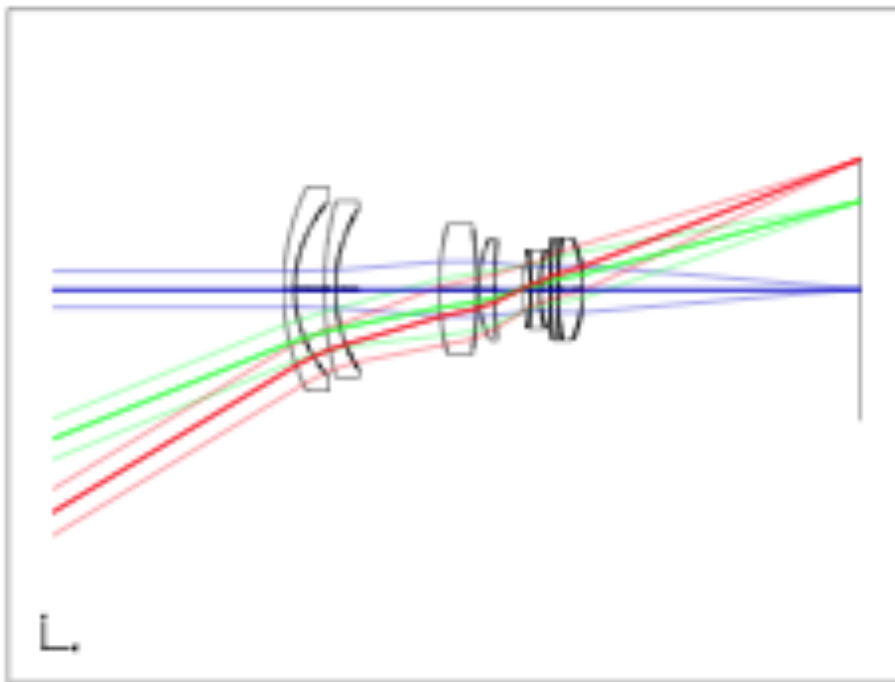
$$\varepsilon = \frac{D_i}{2NA} \Delta\theta_i = D_i \cdot F_n \cdot \Delta\theta_i$$

ε	shift in image position
$\Delta\theta_i$	change in ray angle at element i
D_i	beam diameter at element i (looking at rays from on-axis point)
NA	system numerical aperture (defined at image)
F_n	system focal ratio (defined at image)

J. H. Burge, "An easy way to relate optical element motion to system pointing stability," in *Current Developments in Lens Design and Optical Engineering VII, Proc. SPIE 6288 (2006)*.

How to find D_i

Use footprint diagram to get D_i , beam footprint on element i for on-axis case



Example for tilt of a mirror

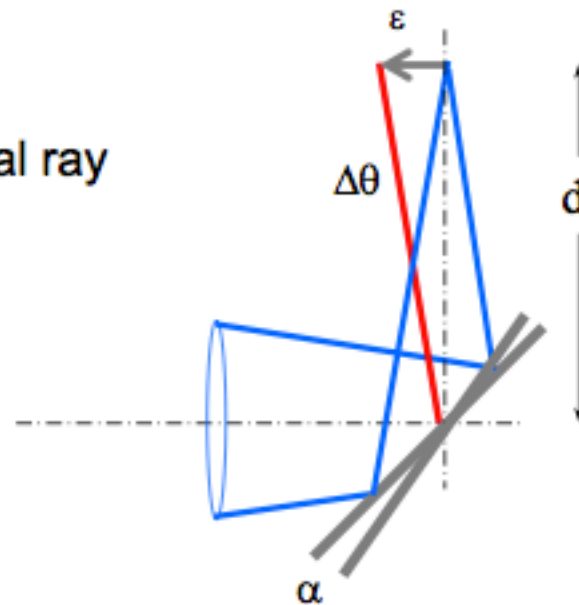
Tilt α causes angular change in central ray $\Delta\theta_i = 2\alpha$

Which causes image motion

$$\varepsilon = 2F_n D_i \cdot \alpha_i$$

“Lever arm” of $2 F_n D_i$ (obvious for case where mirror is the last element)

Follow the central ray



$$\varepsilon = d\Delta\theta$$

Small angle approx

$$= F_n D_i \Delta\theta$$

D_i is beam size
at mirror

$$= 2F_n D_i \alpha$$

This is valid for any mirror!