

## Equations for Calculus Based Physics 53

### Modern Physics

$$x = x' + ut, \quad y = y', \quad z = z', \quad v_x = \frac{dx}{dt}, \quad \Delta t = \gamma \Delta t_0, \quad \gamma = \frac{1}{\sqrt{1-u^2/c^2}}, \quad l = \frac{l_0}{\gamma}, \quad x' = \gamma(x - ut), \quad y' = y,$$

$$z' = z, \quad t' = \gamma(t - ux/c^2), \quad v_x' = \frac{v_x - u}{1 - uv_x/c^2}, \quad \bar{p} = \gamma m \bar{v}, \quad f = f_0 \sqrt{\frac{c+u}{c-u}}, \quad K = (\gamma - 1)mc^2,$$

$$E = K + mc^2 = \gamma mc^2, \quad E^2 = (mc^2)^2 + (pc)^2, \quad (1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots,$$

$$E = hf = h \frac{c}{\lambda}, \quad p = \frac{E}{c}, \quad p = \frac{h}{\lambda}, \quad eV_0 = K_{\max} = hf - \phi, \quad K_{\max} = \frac{1}{2}mv_{\max}^2, \quad hf = E_i - E_f,$$

$$E_n = -\frac{hcR}{n^2}; \quad n=1,2,\dots, \quad r_n = \varepsilon_0 \frac{n^2 h^2}{\pi m e^2} = n^2 a_0, \quad v_n = \frac{1}{\varepsilon_0} \frac{e^2}{2nh}, \quad a_0 = \varepsilon_0 \frac{h^2}{\pi m e^2}, \quad eV_{AC} = hf_{\max} = \frac{hc}{\lambda_{\min}},$$

$$\lambda' - \lambda = \frac{h}{mc}(1 - \cos \phi), \quad I = \sigma T^4, \quad \lambda_m T = 2.90 \times 10^{-3} m.K, \quad I(\lambda) = \frac{2\pi hc^2}{\lambda^5 (e^{hc/\lambda kT} - 1)}, \quad n_i = A e^{-E_i/kT},$$

$$\lambda = \frac{h}{p} = \frac{h}{mv}, \quad mvr = n \frac{h}{2\pi} = n\hbar, \quad p = \sqrt{2meV_{ab}}, \quad \Delta x \Delta p_x \geq \hbar, \quad \Delta E \Delta t \geq \hbar, \quad \Psi(x,y,z,t) = \psi(x,y,z) e^{-iEt/\hbar},$$

$$|\Psi(x,y,z,t)|^2 = (\psi(x,y,z) e^{-iEt/\hbar}) (\psi^*(x,y,z) e^{+iEt/\hbar}), \quad -\frac{\hbar^2}{2m} \frac{d^2}{dx^2} \psi(x) + U(x)\psi(x) = E\psi(x),$$

$$E_n = \frac{n^2 h^2}{8mL^2} = \frac{n^2 \pi^2 \hbar^2}{2mL^2}, \quad \psi_n(x) = \sqrt{\frac{2}{L}} \sin \frac{n\pi x}{L} \quad n=1,2,3,\dots, \quad \int_{-\infty}^{\infty} |\psi(x)|^2 dx = 1,$$

$$T = G e^{-2\kappa L}, \quad G = 16 \frac{E}{U_0} \left(1 - \frac{E}{U_0}\right), \quad \kappa = \frac{\sqrt{2m(U_0 - E)}}{\hbar},$$

$$-\frac{\hbar^2}{2m} \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \psi(x,y,z) + U(x,y,z)\psi(x,y,z) = E\psi(x,y,z); \quad U(r) = -\frac{1}{4\pi\varepsilon_0} \frac{e^2}{r};$$

$$\text{Hydrogen: } E_n = -\frac{1}{(4\pi\varepsilon_0)^2} \frac{m_r e^4}{2n^2 \hbar^2} = -\frac{13.6eV}{n^2}; \quad \text{Hydrogenlike: } E_n = -\frac{Z_{\text{eff}}^2}{n^2} (13.6eV); \quad n=1,2,3,\dots,$$

$$L = \sqrt{l(l+1)}\hbar; \quad l=0,1,2,\dots, \quad L_z = m_l \hbar, \quad m_l = 0, \pm 1, \pm 2, \dots, \quad S = \sqrt{\frac{1}{2} \left( \frac{1}{2} + 1 \right)} \hbar = \sqrt{\frac{3}{4}} \hbar, \quad S_z = m_s \hbar; \quad m_s = \pm \frac{1}{2}$$

$$\bar{J} = \bar{L} + \bar{S}; \quad J = \sqrt{j(j+1)}\hbar; \quad j = \left| l \pm \frac{1}{2} \right|, \quad a = \frac{\varepsilon_0 \hbar^2}{\pi m_r e^2} = 5.29 \times 10^{-11} m, \quad P(r) dr = |\psi|^2 dV = |\psi|^2 4\pi r^2 dr,$$

$$U = -\mu_B B = m_l \frac{e\hbar}{2m} B = m_l \mu_B B; \quad m_l = 0, \pm 1, \pm 2, \dots, \quad n \geq 1; \quad 0 \leq l \leq n-1; \quad |m_l| \leq l; \quad m_s = \pm \frac{1}{2},$$

$$f = (2.48 \times 10^{15} \text{ Hz})(Z-1)^2, \quad E_l = l(l+1) \frac{\hbar^2}{2I}; \quad I = m_r r_0^2; \quad m_r = \frac{m_1 m_2}{m_1 + m_2}; \quad E_n = \left( n + \frac{1}{2} \right) \hbar \sqrt{\frac{k'}{m_r}}$$

$$g(E) = \frac{(2m)^{3/2} V}{2\pi^2 \hbar^3} E^{1/2}, \quad f(E) = \frac{1}{e^{(E-E_f)/kT} + 1}, \quad I = I_s (e^{eV/kT} - 1)$$

$$R = R_0 A^{1/3}, \quad R_0 = 1.2 \times 10^{-15} m, \quad E_B = (ZM_H + Nm_n - \frac{A}{Z} M) c^2, \quad N(t) = N_0 e^{-\lambda t}; \quad T_{\text{mean}} = \frac{1}{\lambda} = \frac{T_{1/2}}{\ln 2}$$

$$E_B = C_1 A - C_2 A^{2/3} - C_3 \frac{Z(Z-1)}{A^{1/3}} - C_4 \frac{(A-2Z)^2}{A} \pm C_5 A^{4/3}$$

$$\text{Constants: } C_1 = 15.75 \text{ MeV}; \quad C_2 = 17.80 \text{ MeV}; \quad C_3 = 0.7100 \text{ MeV}; \quad C_4 = 23.69 \text{ MeV}; \quad C_5 = 39 \text{ MeV}$$

## Some Physical Constants, Conversion Factors, and Experimental Data

Decimal prefixes		Some unit conversion factors		Some experimental data	
<i>centi</i> → 10 <sup>-1</sup>	<i>deca</i> → 10 <sup>1</sup>	1 <i>atm</i> = 1.01325 × 10 <sup>5</sup> <i>Pa</i>		$\rho_{water} = 1000 \text{ kg} / \text{m}^3$	
<i>deci</i> → 10 <sup>-2</sup>	<i>hecta</i> → 10 <sup>2</sup>	1 <i>cal</i> = 4.186 <i>J</i>		$\rho_{air} = 1.20 \text{ kg} / \text{m}^3$	
<i>mili</i> → 10 <sup>-3</sup>	<i>kilo</i> → 10 <sup>3</sup>	1 <i>km</i> = 0.621 <i>mi</i>		$C_V^{air} = 20.8 \text{ J} / \text{mol.K}$	
<i>micro</i> → 10 <sup>-6</sup>	<i>mega</i> → 10 <sup>6</sup>	1 <i>N</i> = 0.225 <i>lb</i>		$p_0 = 1.01 \times 10^5 \text{ Pa}$	
<i>nano</i> → 10 <sup>-9</sup>	<i>giga</i> → 10 <sup>9</sup>	1 <i>gal</i> = 3786 <i>L</i> = 0.003786 <i>m</i> <sup>3</sup>		$m_e c^2 = 0.5109989 \text{ MeV}$	
<i>pico</i> → 10 <sup>-12</sup>	<i>tera</i> → 10 <sup>12</sup>	1.0 <i>mole ideal gas</i> = 22.4 <i>L</i>		$n_{air} = 1.00$	
<i>femto</i> → 10 <sup>-15</sup>	<i>peta</i> → 10 <sup>15</sup>	1 <i>eV</i> = 1.602 × 10 <sup>-19</sup> <i>J</i>		$n_{water} = 1.33$	
		1 <i>u</i> = 1.66053886 × 10 <sup>-27</sup> <i>kg</i>			

### Fundamental constants

$c = 2.99792458 \times 10^8 \text{ m} / \text{s}$	$R = 8.3145 \text{ J} / \text{mol.K}$
$e = 1.6022 \times 10^{-19} \text{ C}$	$R = 0.082 (\text{L.atm}) / (\text{mol.K})$
$G = 6.6742 \times 10^{-11} \text{ N.m}^2 / \text{kg}^2$	$m_e = 9.1093826 \times 10^{-31} \text{ kg}$
$g = 9.80665 \text{ m} / \text{s}^2$	$m_p = 1.67262171 \times 10^{-27} \text{ kg}$
$h = 6.6261 \times 10^{-34} \text{ J.s}$	$m_n = 1.67492728 \times 10^{-27} \text{ kg}$
$h = 4.136 \times 10^{-15} \text{ eV}$	$q_e = -1.60 \times 10^{-19} \text{ C},$
$k = 1.3807 \times 10^{-23} \text{ J} / \text{K}$	$\mu_0 = 4\pi \times 10^{-7} \text{ Wb} / \text{A.m}$
$N_A = 6.0221 \times 10^{23} \text{ molecules} / \text{mol}$	$\epsilon_0 = 1 / \mu_0 c^2 = 8.8541 \times 10^{-12} \text{ C}^2 / \text{N.m}^2$
$a_0 = 5.29 \times 10^{-11} \text{ m},$	$1 / 4\pi\epsilon_0 = 8.98755 \times 10^9 \text{ N.m}^2 / \text{C}^2$
$\sigma = 5.67 \times 10^{-8} \text{ W} / \text{m}^2 . \text{K}^4$	